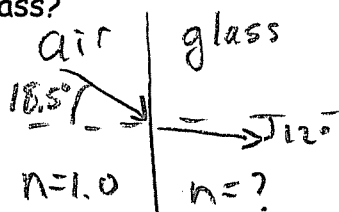


Snell's Law & Critical Angles

1. Light entering a block of glass from air at an angle of incidence of 18.5° leaves the boundary between the air and the glass at an angle of 12.0° . What is the index of refraction of this type of glass?



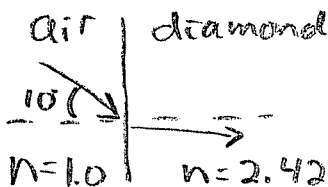
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1.0 \sin 18.5^\circ = n_2 \sin 12^\circ$$

$$.317 = n_2 (.208)$$

$$n_2 = \frac{.317}{.208} = 1.52$$

2. Light from air is incident on diamond at an angle of 10.0° . At what angle will it refract?



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1.0 \sin 10^\circ = 2.42 \sin \theta_2$$

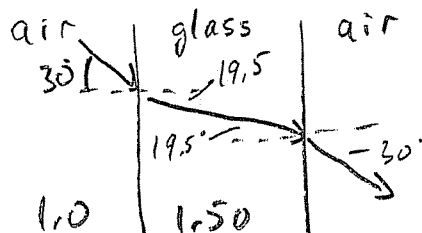
$$.174 = 2.42 \sin \theta_2$$

$$\sin \theta_2 = .071$$

$$\theta = \sin^{-1}(.071)$$

$$= 4.1^\circ$$

3. A beam of light is incident on a sheet of glass in a window at an angle of 30° . Describe exactly what path the light beam will take (a) as it enters the glass and (b) as it leaves the other side of the glass. Assume $n=1.500$.



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

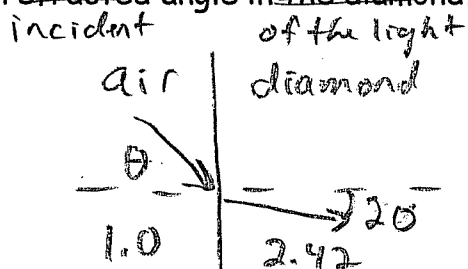
$$1.0 \sin 30 = 1.5 \sin \theta_2$$

$$.5 = 1.5 \sin \theta_2$$

$$.333 = \sin \theta$$

$$\sin^{-1}(.333) = 19.5^\circ$$

4. Light traveling in air has an angle of incidence of 40° as it passes into diamond. What is the refracted angle in the diamond?



refraction 20

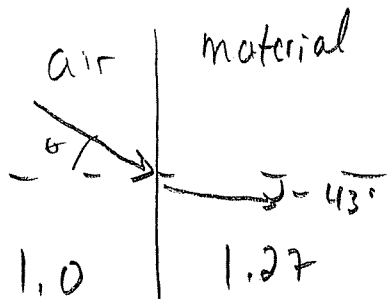
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1.0 \sin \theta_1 = 2.42 \sin 20^\circ$$

$$\sin \theta = .828$$

$$\sin^{-1}(.828) = 56^\circ$$

5. A transparent material has a refractive index of 1.27. What is the angle of incidence in air when the angle of refraction in the substance is 43° ?



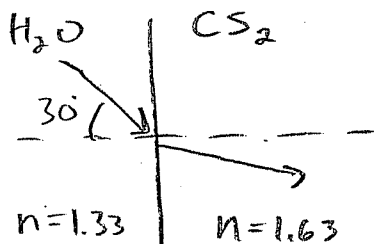
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1.0 \sin \theta = 1.27 \sin 43^\circ$$

$$\sin \theta = .866$$

$$\theta = 60^\circ$$

7.6 A ray of light passes from water into carbon disulphide ($n=1.63$) with an angle of incidence of 30° . What is the angle of refraction in the carbon disulphide?



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

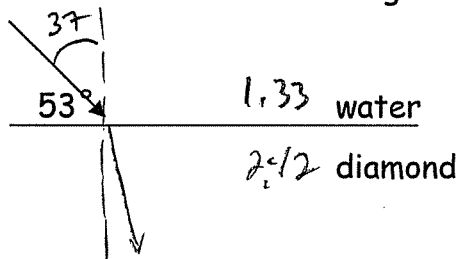
$$1.33 \sin 30^\circ = 1.63 \sin \theta_2$$

$$.665 = 1.63 \sin \theta_2$$

$$\sin \theta_2 = .408$$

$$\theta_2 = 24^\circ$$

8.7 Using Snell's Law with $n = 1.33$ for water and $n = 2.42$ for diamond determine the angle of refraction in the diamond for the following situation.



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

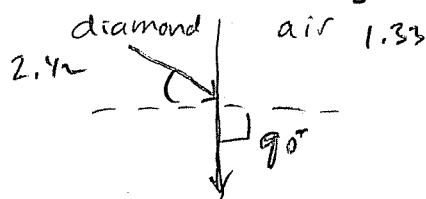
$$1.33 \sin 53^\circ = 2.42 \sin \theta_2$$

$$.8 = 2.42 \sin \theta_2$$

$$.33 = \sin \theta_2$$

$$\theta_2 = 19.3^\circ$$

11.6 Calculate the critical angle for diamond into air.



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

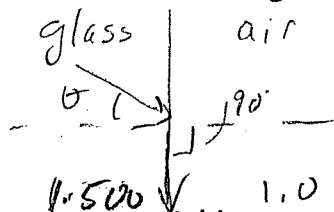
$$2.42 \sin \theta_c = 1.33 \sin 90^\circ$$

$$\sin \theta_c = \frac{1.33}{2.42} = .549$$

$$\theta_c = \sin^{-1}(.549)$$

$$\theta_c = 33^\circ$$

12.9 What is the critical angle for a glass into air that has an index of refraction of 1.500?



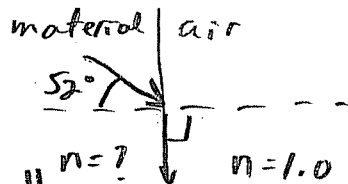
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$1.500 \sin \theta_c = 1.0 \sin 90^\circ$$

$$\sin \theta_c = \frac{1}{1.500}$$

$$\theta_c = 42^\circ$$

13. A certain material has a critical angle of 52.0° . What is its index of refraction?



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$n \sin 52^\circ = (1)(\sin 90^\circ)$$

14. What is the velocity of light in quartz? $n = \frac{1}{.788} = 1.30$

$$n = \frac{v_{vac}}{v_{med}}$$

$$1.54 = \frac{3 \times 10^8}{v_{med}}$$

$$v_{med} = \frac{3 \times 10^8}{1.54} = 1.95 \times 10^8 \text{ m/s}$$

Answers: 1. $n_r = 1.53$ 2. $r = 4.1^\circ$ 3. $r = 19.5^\circ$ 4. $r = 30.0^\circ$ 5. $i = 60.0^\circ$ 6. $n_r = 1.19$ 7. $r = 24.1^\circ$ 8. $r = 19.3^\circ$ 9. $r = 55.7^\circ$ 10. $n = 1.41$ 11. $l = 5.60 \times 10^{-7} \text{ m}$ 12. $i_c = 24.4^\circ$ 13. $n = 1.27$ 14. $f = 4.29 \times 10^{14} \text{ Hz}$ 15. $2.244 \times 10^8 \text{ m/s}$, $4.41 \times 10^{-7} \text{ m}$